

Algebraic Methods

Algebra: the word was derived from the title of **Al-Khwarizmi's** book (written in Baghdad ca. **820 A.D.**), “**Hisab al-jabr w'al-muqabala**” which means (roughly) “**Calculation by restoration and reduction**”.

– book was later called “**Al-Khwarizmi's Algebra**”.

al-jabr (= **restoration**): add equal terms to both sides of an equation (to eliminate negative terms)

al-muqabala (= **reduction**): subtract equal terms to both sides of an equation (to simplify it).

Due to the popularity of Al-Khwarizmi's book, the term **algebra** came to mean:

Algebra = “**art** of **reducing and solving equations**”.

Note: From the very beginning, **algebra** (and **mathematics** in general) was considered to be a **great art**:

Omar Khayyam (1080): **The Art of Algebra**.

Cardano (1545): **Ars Magna** (= **The Great Art**).

In this course we'll study various methods to solve equations in many different **number systems**.

Method: from the Greek word *méthodos* = a way or path of an investigation according to fixed rules (*hódos* = way).

– usually: **systematic procedure** (for solving a problem). Thus, the term is closely related to:

Algorithm: The description of a (finite) procedure (usually: suitable for programming on a computer).

– derived from **Al-Khwarizmi**'s name, and is closely connected with the advent of the so-called **Arabic numerals** (and the **decimal notation**) in Europe.

– due to the fact that **Al-Khwarizmi** wrote a book on **Indian numerals** called

Algorithmi de numero indorum

(**Calculation with Indian numerals**)

in its **Latin** translation (the original **Arabic** version no longer exists).

Note: **Algorism** means **decimal notation**.