1. Put these matrices into row reduced echelon form:

(a)	[ 1	2	3]	(b)	0	2	3]	(a)	1	2	3]	(4)	. 1	2	3]
	4	5	6	(0)	2	4	6	(C)	2	4	6	(u)	0	0	6

2. Find the polynomial of degree 3 [a polynomial of the form  $f(t) = a + bt + ct^2 + dt^3$ ] which passes through the points (0, 1), (1, 0), (-1, 0) and (2, -15).

3. Find, using Gauss-Jordan elimination, and showing all the steps, all the solutions to

$$x_1 - 7x_2 + x_5 = 3$$
  

$$x_3 - 2x_5 = 2$$
  

$$x_4 + x_5 = 1$$

Be careful setting up the matrix correctly!

4. Solve the famous *Hundred Fowl Problem* (Prob. 60 in §2): "A rooster is worth five coins, a hen three coins, and 3 chicks one coin. With 100 coins we buy 100 of them. How many roosters, hens, and chicks can we buy?"

Let r be the number of roosters, h the number of hens, and c the number of chicks that we buy.

- (a) Write down the equations specified by the problem.
- (b) If r, h, and c can be arbitrary real numbers, find all solutions to the equations in part (a).
- (c) If r, h, and c have to be positive integers (i.e., whole numbers), and c has to be a multiple of 3, find all the solutions.
- 5. For what values of k and  $\ell$  does the augmented system

$$\begin{bmatrix} 1 & 1 & -2 & | & 1 \\ 2 & k & 1 & | & 2 \\ 1 & 10 & k & | & \ell \end{bmatrix}$$

have

- (a) Exactly one solution?
- (b) No solutions?
- (c) Infinitely many solutions?

Find all the solutions in case (c).