

**Math 231, Introduction to Differential Equations, Fall 2011**

**Queen's University, Department of Mathematics**

**Homework 1, Due Thursday September 23**

1. Find the solution of the following initial value problem

$$\frac{dy}{dt} + y \cos(t) = 4 \cos(t), \quad y(\pi) = -1.$$

2. Consider the following initial value problem

$$\frac{dy}{dx} = \frac{x^2 + 3y^2}{2xy}, \quad y(1) = -1.$$

- a). Show that this equation is homogeneous (see page 49 Boyce and DiPrima, 8th or 9th edition).

- b). Substituting the homogeneous variable  $v = \frac{y}{x}$ , calculate  $\frac{dv}{dx}$ , and find the general solution of the new differential equation in the  $x - v$  plane. Graph some of the solution curves in the variables  $x, v$ , indicating carefully where vertical tangencies might occur.

- c). Find the unique solution (in the  $x, y$  variables) to the initial value problem given at the beginning.

3. Find the family of curves which are the *orthogonal trajectories* for the family of hyperbolas

$$x^2 - 2y^2 = c$$